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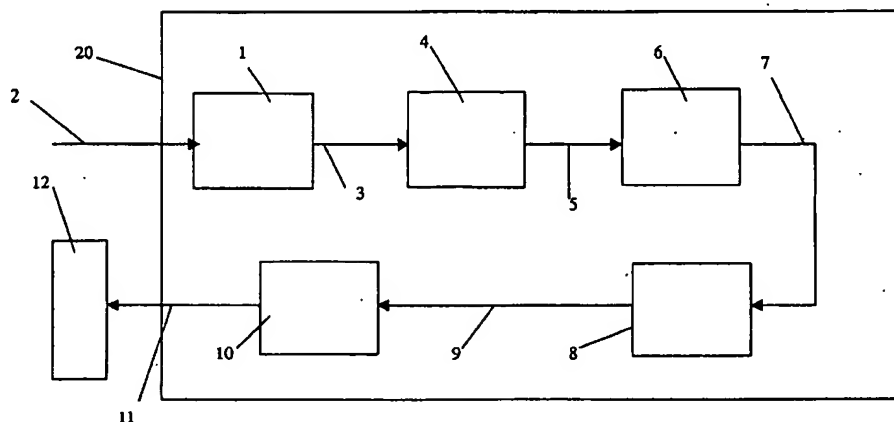
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(54) Title: **HOLOGRAPHIC APPARATUS AND METHOD**



(57) Abstract: The invention relates to a method of and apparatus for displaying a holographically generated video image having plural video frames. For each period there is provided a respective sequential plurality of holograms. The holograms of the plural video frames are displayed for viewing the replay field thereof, and the noise variance of each frame is perceived as attenuated by averaging across said plurality of holograms.

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Holographic Apparatus and Method

The present invention relates to a method of displaying a holographically generated video image composed of plural video frames, and to apparatus constructed and arranged to display a holographically generated video image having plural video frames.

For the sake of clarity, the term "video data" is not limited to data representing any particular type of image content and is intended to include data that is representative of one or more still images, wherein the data are periodically or regularly refreshed.

Holographically generated 2D video images are known to possess significant advantages over their conventionally projected counterparts, especially in terms of definition and efficiency. However, the computational complexity of the current hologram generation algorithms preclude their use in real-time applications. Furthermore, even if the existing algorithms were fast enough, the images generated by them are not of sufficient quality for use in a display application.

Traditionally, hologram generation algorithms may proceed by finding holograms that minimise the mean-squared error (MSE) between the desired image and the image produced (the replay field, or RPF) when the hologram is illuminated with coherent light. The inventors have shown that human subjects consider lower signal and noise variance in the RPF to be far more important in display applications. Using this result, a new algorithm optimised to the psychometrically-determined perceptual measure of image quality has been developed.

Holographically generated images may be formed by light leaving a device exhibiting a phase-modulating effect upon light incident upon the device. Typically the device is a spatial light modulator (SLM) and has a field of addressable phase-modulating elements. In some SLMs the phase-modulating elements are a linear or one-

dimensional array of elements; in others a two dimensional array may be provided. For simplicity many SLMs have a regular 2-D. array of like, generally square, phase-modulating elements; it is however not necessary for the phase-modulating elements to be alike in size or shape.

5

In general the phase-modulating elements of SLMs are often referred to as "pixels", and the elements themselves as "pixellated". The terms are used interchangeably herein. It is not intended herein, when the term "pixel" is used, that any directly viewable picture content is to be seen on the elements concerned.

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An object of some embodiments of the invention is to achieve high quality real-time holographic video projection.

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An object of some embodiments of the invention is to provide an algorithm for forming a CGH, which algorithm involves a low number of computationally intensive steps.

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An object of some embodiments of the invention is to provide a fast algorithm for forming a CGH, which algorithm can be implemented on relatively unsophisticated hardware, such as is currently commercially available.

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According to one aspect of the invention there is provided a method of displaying a holographically-generated video image composed of plural video frames, the method comprising providing for each frame period a respective sequential plurality of holograms and displaying the holograms of the plural video frames for viewing the replay field thereof, whereby the noise variance of each frame is perceived as attenuated by averaging across said plurality.

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In an embodiment the providing step comprises generating each hologram by implementing an algorithm having a single computationally intensive step.

In an embodiment the single step is a Fourier transform step.

5 In an embodiment the algorithm is arranged, for each said plurality of pixellated holograms, to a) form first data having amplitude equal to the amplitude of the desired pixel and identically distributed uniformly random phase; b) inverse Fourier transform the first data to provide second data; c) shift the second data in the real direction in the complex plane sufficiently to form a third data set in which the phase of each data point is small; d) form as a fourth data set the magnitude of the third data set; and e)
10 binarise the fourth data set to form a fifth data set for display as a said hologram.

In an embodiment the step of binarisation comprises thresholding about the median of the fourth data set whereby the fifth data set has dc balance and low reconstruction error.

15

In another embodiment the step of binarisation comprises thresholding the fourth data set about zero.

20 In an embodiment the display device comprises a spatial light modulator having a pixellated phase mask imposing phase shifts of substantially 0 and $\pi/2$, wherein the effect of the display device showing a binary hologram in co-operation with the two-phase phase mask simulates a four-phase modulation, wherein each pixel has one of the values $[1, j, -1, -j]$. Other phase shifts would be possible provided a difference of substantially $\pi/2$ or $n \pi/2$ is present between the two levels.

25

In an embodiment the pixel values of the phase mask are spatially random.

In another embodiment, the pixel values of the phase mask are decided deterministically.

30

In an embodiment step b) comprises inverse Fourier transforming and applying the phase mask values to the first data to provide the second data.

5 An alternative family of embodiments uses a Fresnel transformation instead of a Fourier transform.

Some embodiments are restricted to 2D holograms; others provide 3D.

10 According to another aspect of the invention there is provided apparatus constructed and arranged to display a holographically-generated video image having plural video frames, the apparatus having processing means arranged to provide for each frame period a respective sequential plurality of holograms and a display device arranged to receive the sequential plurality of holograms of each frame and to display the holograms of the plural video frames of the video image for viewing the replay field
15 thereof, whereby the noise variance of each frame is perceived as attenuated by averaging across said plurality of holograms.

In an embodiment the processing means is arranged to generate each said hologram by implementing an algorithm having a single computationally intensive step.

20

In an embodiment the single step is a Fourier transform step.

In an embodiment the algorithm is arranged, for each said plurality of pixellated holograms, to a) form first data having amplitude equal to the amplitude of the desired
25 image pixels and identically distributed uniformly random phase; b) inverse Fourier transform the first data to provide second data; c) shift the second data in the real direction in the complex plane sufficiently to form a third data set in which the phase of each data point is small; d) form as a fourth data set the magnitude of the third data set; and e) binarise the fourth data set to form a fifth data set for display as a said
30 hologram.

In an embodiment the step of binarisation comprises thresholding about the median of the fourth data set whereby the fifth data set has dc balance and low reconstruction error.

- 5 In another embodiment, the thresholding of the fourth data set is performed about zero.

10 In an embodiment the display device comprises a spatial light modulator having a pixellated phase mask imposing phase shifts of substantially 0 and $\pi/2$, wherein the effect of the display device showing a binary hologram in co-operation with the two-phase phase mask simulates a four-phase modulation, wherein each pixel has one of the values $[1, j, -1, -j]$. Other phase shifts would be possible provided a difference of substantially $\pi/2$ or $n \pi/2$ is present between the two levels.

- 15 In an embodiment the pixel values of the phase mask are spatially random.

In an embodiment step b) comprises inverse Fourier transforming and applying the phase mask values to the first data to provide the second data.

- 20 Embodiments of the hologram generation algorithm / method can be run sufficiently fast to provide a number, e.g. 40, holograms per video frame, where a video frame is 1/25 second. It has been found that there is a statistical result that the noise variance of the time average of N images, each with independent noise of some arbitrary distribution, falls as $1/N$. Embodiments of a first algorithm embodying the invention
- 25 can therefore generate, in real time, a set of N holograms per video frame ('subframes') to produce RPFs with independent noise. If the frames are displayed quickly enough then the limited temporal bandwidth of the eye is exploited to impart the effect of noise variance attenuation due to averaging. Embodiments of a second algorithm can produce $2N$ holograms from N Fourier steps.

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According to a further aspect of the invention there is provided a method of providing a pixellated hologram comprising forming first data having amplitude equal to the amplitude of the desired image pixels; inverse Fourier transforming the first data to provide second data; shifting the second data in the real direction in the complex plane sufficiently to form a third data set in which the phase of each data point is small; forming as a fourth data set the magnitude of the third data set; and binarising the fourth data set to form a fifth data set for display as said hologram.

According to a yet further aspect of the invention there is provided a method of providing a pixellated hologram comprising forming first data having amplitude equal to the amplitude of the desired image pixels; inverse Fresnel transforming the first data to provide second data; shifting the second data in the real direction in the complex plane sufficiently to form a third data set in which the phase of each data point is small; forming as a fourth data set the magnitude of the third data set; and binarising the fourth data set to form a fifth data set for display as said hologram.

According to still another aspect of the invention there is provided a method of generating a pixellated holograms, the method comprising forming a first data set, the members of said first data set having respective amplitudes equal to the amplitudes of respective desired pixels; performing an inverse Fourier transform on the first data set to provide second data set; shifting the second data set in the real direction in the complex plane sufficiently to form a third data set in which the phase of each data point is small; forming as a fourth data set the magnitude of the third data set; and binarising the fourth data set to form a fifth data set for display as a said hologram.

The forming step may comprise forming data having identically distributed random phase.

The step of binarisation may comprise thresholding about the median of the fourth data set whereby the fifth data set has dc balance and low reconstruction error.

The display device may comprise a spatial light modulator having a pixellated phase mask imposing phase shifts of substantially 0 and $\pi/2$, wherein the effect of the display device showing a binary hologram in co-operation with the two-phase phase mask
5 simulates a four-phase modulation, wherein each pixel has one of the values $[1, j, -1, -j]$. Other phase shifts would be possible provided a difference of substantially $\pi/2$ or $n \pi/2$ is present between the two levels.

The pixel values of the phase mask may be spatially random.
10

The method may further comprise applying the phase mask values to the first data to provide the second data.

The image may be a 2 dimensional image. Alternatively the image may be three
15 dimensional.

Exemplary embodiments of the invention will now be described with reference to the accompanying drawings in which

Figure 1 shows a block schematic drawing of apparatus embodying the
20 invention;

Figure 2a shows a conjugate image present due to binary SLM;

Figure 2b shows the conjugate image eliminated with phase mask;

Figure 2c shows the conjugate image eliminated using Fresnel holography

Figure 3a shows an exemplary replay field produced by an embodiment of a
25 method of the invention;

Figure 3b shows a replay field similar to that of Figure 3a but produced by direct binary search.

Figure 4 shows a partial cross-sectional view through an SLM having a pixellated
30 phase mask imposing phase shifts of 0 and $\pi/2$.

Referring to Figure 1, a signal (2) representing an $p \times q$ pixel input intensity field T_{xy} , generated directly from a video signal is input to a processing device (20) having a first processing block (1). The processing device (20) in this embodiment includes a field programmable gate array (FPGA) running code to enable it to perform the required functions. In other embodiments an ASIC is used and in yet others a programmed general purpose computer is used. The first processing block (1) for each said plurality of pixellated holograms, forms a first data set $T_{xy}^{(n)}$ at an output (3) by the expression $T_{xy}^{(n)} = \sqrt{T_{xy}} \exp(j\Phi_{xy}^{(n)})$, so that the first data set $T_{xy}^{(n)}$ has amplitude equal to the amplitude of the desired pixel and identically distributed (i.i.d.) uniformly random phase.

The first data set (3) is applied to a second processing block (4) which forms a second data set $G_{xy}^{(n)}$ such that $G_{xy}^{(n)} = F^{-1}[T_{xy}^{(n)}]$ at output (5) where F^{-1} represents the 2D inverse Fourier transform.

The second data set is then shifted by third processing block (6) in the real direction in the complex plane (i.e. to the right) sufficiently to form a third data set (7) in which the phase of each data point is small. The third processing block (6) forms R as the smallest positive real such that $|G_{xy}^{(n)}| \leq R \quad \forall x, y, n$. and adds a real α where $\alpha \gg R$ to each data item of the second set to form a third set $\alpha + G_{xy}^{(n)}$ at output (7).

The third data set at output (7) is applied to a magnitude-forming fifth processing block (8) performing the function $M_{xy}^{(n)} = |\alpha + G_{xy}^{(n)}|$ such that $M_{xy}^{(n)}$ is output as a fourth data set (9).

The fourth data is then supplied to a binarisation stage (10) performing the function

$$H_{xy}^{(n)} = \begin{cases} -1 & \text{if } M_{xy}^{(n)} < Q^{(n)} \\ 1 & \text{if } M_{xy}^{(n)} \geq Q^{(n)} \end{cases} \quad \text{where } Q^{(n)} = \text{median}(M_{xy}^{(n)}) \text{ to form a fifth data set (11)}$$

for display as a said hologram.

- 5 The fifth data set (11) is supplied to a ferroelectric liquid crystal SLM (12) for display and viewing. Although a ferroelectric liquid crystal spatial light modulator is used in this embodiment other devices, for example including nematic SLMs, OASLMs (optically-addressed spatial light modulators), and also more exotic types of liquid crystal displays such as electroclinic, pi cell, flexoelectric, antiferroelectric, 10 ferroelectric, V-shaped switching cells, and guest-host dye cells may be substituted, in addition to non-liquid crystal technologies such as OLED displays, vacuum fluorescent displays, electroluminescent displays, MEMS devices such as DMDs. The device may be transmissive or reflective.

- 15 The presence of only a single computationally intensive step, i.e. the inverse Fourier transform, allows current hardware to generate in real time plural, e.g. 40, holograms per video frame.

- In a second embodiment, a modified process generates sets of $2N$ distinct $p \times q$ binary phase holograms $H_{xy}^{(n)}$, each of which produces a replay field that approximates the 20 same target image. The key feature of the process is that the noise fields produced by each hologram are i.i.d., satisfying the conditions above.

- The process begins with the specification of a target intensity image T_{xy} and proceeds 25 as follows:

1. Let $T_{xy}^{(n)} = \sqrt{T_{xy}} \exp(j\Phi_{xy}^{(n)})$ where $\Phi_{xy}^{(n)}$ is uniformly distributed between 0 and 2π for $1 \leq n \leq N$, $1 \leq x \leq p$, $1 \leq y \leq q$

2. Let $G_{xy}^{(n)} = F^{-1}[T_{xy}^{(n)}]$ where F^{-1} represents the 2D inverse Fourier transform operator, for $1 \leq n \leq N$
3. Let $M_{xy}^{(n)} = \Re\{G_{xy}^{(n)}\}$ for $1 \leq n \leq N$
4. Let $M_{xy}^{(n+N)} = \Im\{G_{xy}^{(n)}\}$ for $1 \leq n \leq N$
5. Let $H_{xy}^{(n)} = \begin{cases} -1 & \text{if } M_{xy}^{(n)} < Q^{(n)} \\ 1 & \text{if } M_{xy}^{(n)} \geq Q^{(n)} \end{cases}$ where $Q^{(n)} = \text{median}(M_{xy}^{(n)})$ and $1 \leq n \leq 2N$.

Steps 3 and 5 of this process are exactly equivalent to steps 3, 4 and 5 of the first embodiment, but an additional step (number 4 in this process) is added. The holograms $M_{xy}^{(n)}$ produced here are thus exactly the same as the holograms $M_{xy}^{(n)}$ produced by the original algorithm, only here the holograms $M_{xy}^{(n+N)}$ are also provided “for free” –i.e. without a need for further Fourier transform step.

Step 1 forms N targets $T_{xy}^{(n)}$ equal to the amplitude of the supplied intensity target T_{xy} , but with i.i.d. uniformly-random phase. Step 2 computes the N corresponding full complex Fourier transform holograms $G_{xy}^{(n)}$. Steps 3, 4 compute the real part and imaginary part of the holograms, respectively. Binarisation of each of the real and imaginary parts of the holograms is then performed in step 5: thresholding around the median of $M_{xy}^{(n)}$ ensures equal numbers of -1 and 1 points are present in the holograms, achieving DC balance (by definition) and also minimal reconstruction error. Hence, for one Fourier transform operation performed upon T_{xy} , two binary phase holograms H_{xy} are provided as opposed to one hologram obtained using the process of the first embodiment.

In another embodiment, steps 3-5 perform not a binary quantisation but a quantisation to more than two phase levels. In the latter case, only one hologram is produced per Fourier transform performed upon T_{xy} .

- 5 Any purely real hologram (such as a binary phase hologram employed in some embodiments) produces a conjugate image in the replay field, reducing the usable area and hence the efficiency by half.

10 The conjugate image can be removed by generating a four-phase hologram where each pixel takes one of the values $[1, j, -1, -j]$, although such holograms cannot be displayed on an inherently binary device such as a ferroelectric SLM. More than two phase levels can be displayed on a nematic liquid crystal device, but commercially-available device of this type are currently too slow for high frame-rate applications, as provided by the algorithm described above.

15 However by etching a pixellated phase mask of pixel values 1 and j (thus imposing phase shifts of 0 and $\pi/2$ respectively) on the top surface of a binary-phase SLM the conjugate image can be removed. This is achieved by randomly setting the pixel values of the mask such that the net modulation imposed by the combination of the
20 SLM and phase mask lie in the set $[1, j, -1, -j]$, which provides the extra degree of freedom required to remove the conjugate image (at the expense of additional RPF noise), despite the fact that the SLM itself is binary. This technique has been used in correlator design and is here applied to the display application. Although the pixel values of the mask are random, and thus have "dc balance" in that there are
25 statistically equal numbers of each value of phase shift, the mask itself is fixed and the pixel position of each value of phase shift is known.

In other embodiments, a distribution of phase shifts that is not completely random is used.

30

To modify the algorithm described above to use a phase mask, the second block (4) is modified to provide a $G_{xy}^{(n)}$ such that

$$G_{xy}^{(n)} = \frac{F^{-1}[T_{xy}^{(n)}]}{P_{xy}}$$

where P_{xy} defines the phase mask, which has been generated randomly so that each pixel has an equal probability of taking the value 1 or j .

Referring to Figure 4, a cross-sectional view through a part of a binary SLM (100) is shown. The SLM (100) has plural pixels (120-123) in the drawing although it will be understood that the pixels are in fact arranged in a two dimensional matrix. Each pixel (120-123) is capable of being electrically controlled so as to provide a phase shift of 0 or π . Each pixel (120-123) of the SLM has a respective phase-mask pixel (130-133) overlying it and disposed in correspondence with it. As will be seen in the Figure the first, third and fourth phase mask pixels (130, 132, 133) have a relatively low thickness whereas the second phase mask pixel (131) has a relatively high thickness. The thickness difference is selected on the basis of the material of the phase mask and on the basis of the wavelength of the light used. The selection is such that the light passing through the thicker pixels (131) is subject to a phase shift of π more than the light passing through the thinner pixels (130,132,133).

Where the SLM or like device is reflective, the light will pass twice through the phase mask, and corresponding changes in thickness will be needed.

In the present embodiment the phase mask is formed as a coating on the SLM (100). It would of course be possible to use other arrangements for example use two substantially identical SLMs with one providing a data display and the other forming the phase mask.

13

To evaluate the efficacy of this technique in simulation, holograms were generated for the two test patterns with each hologram being replicated twice, the replication step being performed between steps 2 and 3 in the algorithm. The replay fields formed demonstrated that the conjugate image is removed effectively.

5

The foregoing discussion relates to producing desired 2D structure in the far field using Fourier holograms. The method can also be extended to produce Fresnel holograms for the production of structure in the near field, which is particularly useful for a lensless optical configuration. Fresnel holography offers a further advantage of enabling lensless projection, since the hologram itself encodes the focussing element, giving an obvious weight, cost and size saving over conventional projective display systems.

The discrete Fresnel transform is closely related to the Fourier transform, and describes the near field T_{xy} produced at distance f by the hologram G_{xy} (of dimensions X by Y and corresponding pixel sizes Δ_x and Δ_y) when illuminated with coherent light of wavelength λ . When imaging not too close to the hologram the transform is given by

20

with corresponding inverse transform

$$T_{xy} = \frac{j}{\lambda f} \exp \left(-j\pi\lambda f \left[\frac{x^2}{X^2\Delta_x^2} + \frac{y^2}{Y^2\Delta_y^2} \right] \right) \times F \left[G_{xy} \exp \left(\frac{-j\pi}{\lambda f} (x^2\Delta_x^2 + y^2\Delta_y^2) \right) \right]$$

$$G_{xy} = \exp \left(\frac{j\pi}{\lambda f} (x^2\Delta_x^2 + y^2\Delta_y^2) \right) \times F^{-1} \left[T_{xy} \frac{\lambda f}{j} \exp \left(j\pi\lambda f \left[\frac{x^2}{X^2\Delta_x^2} + \frac{y^2}{Y^2\Delta_y^2} \right] \right) \right]$$

Hence if processing block (4) provides a $G_{xy}^{(n)}$ such that

$$G_{xy} = \exp \left(\frac{j\pi}{\lambda f} (x^2\Delta_x^2 + y^2\Delta_y^2) \right) \times F^{-1} \left[T_{xy} \frac{\lambda f}{j} \exp \left(j\pi\lambda f \left[\frac{x^2}{X^2\Delta_x^2} + \frac{y^2}{Y^2\Delta_y^2} \right] \right) \right]$$

25

Fresnel holograms are generated that form the target image at the specified distance f from the hologram.

5 The techniques described may be modified for the generation of 3D holograms for 3D holographic video display. A 3D hologram of an object is simply a recording of the complex electromagnetic field (produced by light scattered by the object) at a plane in front of the object. By Huygens' principle, if the EM field distribution on a plane P is known, Huygens wavelets can be propagated through space to evaluate the field at any point in 3D space. As such, the plane hologram encodes all the information necessary
10 to view the object from any position and angle in front of the plane and hence is, in theory, optically indistinguishable from the object. In practice, limitations in the pixel resolution of the recording medium restricts the viewing angle θ which, as in the 2D case, varies inversely with the pixel size Δ .

15 Consider a plane, perpendicular to the z -axis, intersecting the origin, and one point source emitter of wavelength λ and amplitude A at position (X, Y, Z) behind it. The field F present at position (x, y) on the plane – i.e. the hologram – is given by

$$F(x, y) = \frac{ZA}{j\lambda r^2} \exp\left(\frac{2\pi j}{\lambda} r\right) \text{ with } r = \sqrt{(x - X)^2 + (y - Y)^2 + Z^2}$$

20 If a 3D scene is regarded as M sources of amplitude A_i at (X_i, Y_i, Z_i) , the linear nature of EM propagation results in the total field hologram F being

$$F(x, y) = \sum_{i=1}^M \frac{Z_i A_i}{j\lambda r_i^2} \exp\left(\frac{2\pi j}{\lambda} r_i\right) \text{ with } r_i = \sqrt{(x - X_i)^2 + (y - Y_i)^2 + Z_i^2}$$

If $F(x, y)$ is to be sampled over the region $x_{\min} \leq x \leq x_{\max}$, $y_{\min} \leq y \leq y_{\max}$ to form an $m \times m$ hologram F_{xy} , there is obtained:

$$F_{xy} = \sum_{i=1}^M \frac{Z_i A_i}{j\lambda r_i^2} \exp\left(\frac{2\pi j}{\lambda} r_i\right)$$

$$\text{with } r_i = \sqrt{\left(x_{\min} + x \frac{x_{\max} - x_{\min}}{m} - X_i\right)^2 + \left(y_{\min} + y \frac{y_{\max} - y_{\min}}{m} - Y_i\right)^2 + Z_i^2}$$

There is thus presented an algorithm (with an SLM phase mask) that generates N full-parallax 3D holograms $H_{xy}^{(n)}$ for a given array of point sources, as above.

Let $F_{xy}^{(n)} = \sum_{i=1}^M \frac{Z_i A_i}{j \lambda r_i^2} \exp\left(\Phi_i^{(n)} j + \frac{2\pi j}{\lambda} r_i\right)$ with r_i as above where $\Phi_i^{(n)}$ is uniformly distributed between 0 and 2π for $1 \leq n \leq N, 1 \leq i \leq M$

5

Let $G_{xy}^{(n)} = \frac{F_{xy}^{(n)}}{P_{xy}}$, where P_{xy} is the precomputed $[1, j]$ phase mask as described in the previous section.

Let R be the smallest positive real such that $|G_{xy}^{(n)}| \leq R \quad \forall x, y, n$. R exists since each value taken by $G_{xy}^{(n)}$ is finite and so $G_{xy}^{(n)}$ has compact support

10

Let $M_{xy}^{(n)} = |\alpha + G_{xy}^{(n)}|$, where α is real and very much greater than R .

Let $H_{xy}^{(n)} = \begin{cases} -1 & \text{if } M_{xy}^{(n)} < Q^{(n)} \\ 1 & \text{if } M_{xy}^{(n)} \geq Q^{(n)} \end{cases}$ where $Q^{(n)} = \text{median}(M_{xy}^{(n)})$

Alternatively, to obtain two holograms per Fourier transform then the preceding three steps are replaced by the following:

15

Let $M_{xy}^{(n)} = \Re\{G_{xy}^{(n)}\}$ for $1 \leq n \leq N$

Let $M_{xy}^{(n+N)} = \Im\{G_{xy}^{(n)}\}$ for $1 \leq n \leq N$

Let $H_{xy}^{(n)} = \begin{cases} -1 & \text{if } M_{xy}^{(n)} < Q^{(n)} \\ 1 & \text{if } M_{xy}^{(n)} \geq Q^{(n)} \end{cases}$ where $Q^{(n)} = \text{median}(M_{xy}^{(n)})$ and $1 \leq n \leq 2N$

20 To test this algorithm, there is considered the calculation of $N = 8$ holograms of resolution 512×512 and size $2\text{mm} \times 2\text{mm}$ centred at the origin of plane P , giving a pixel size of $\Delta = 4\mu\text{m}$ and hence a viewing angle of around 9 degrees under coherent red illumination ($\lambda = 632\text{nm}$). The 3D scene used was a set of 944 point sources that

formed a wireframe cuboid of dimensions $12\text{cm} \times 12\text{cm} \times 18\text{cm}$, located at a distance of 1.91m from the plane.

5 The simulated RPFs produced were calculated by propagating Huygens wavelets from the N holograms in turn through a pinhole aperture K onto a virtual screen (a plane perpendicular to the line from the centre of the cube to the pinhole), and recording the time-averaged intensity distribution on the screen.

10 Unfortunately, in contrast with algorithm described for 2D, the computation of step one in the 3D algorithm above may not be realisable in real time with current consumer hardware for a scene with anything but a very small number of point sources. However, the required holograms generated by the algorithm can be computed and stored for recall in real time. Much more powerful computation may be needed for real-time three-dimensional hologram generation, although it has been
15 found possible to optimise the calculations in a way that suggests that such computation may not be needed.

The holographic projection method detailed above is realisable in hardware. At the time of writing, commercially available FPGAs (field programmable gate arrays) and
20 other programmable hardware such as DSPs can be programmed using commercially available or custom code to compute 512×512 Fourier transforms at a rate of at least 2400 frames/sec, sufficient for full-colour video (25 frames/sec, 3 colour planes, $N = 32$). For the display device, a commercially available SLM can display a sufficient frame rate at at least 512×512 resolution. It is possible to use separate illumination
25 devices where multiple colours are needed –for example for a full colour display. Alternatively a single device capable of multiple colour output can be used instead. Two significant design issues have been identified.

30 Firstly, since optical loss in the phase holographic element is small and total energy is conserved, nearly all of the incident optical energy is routed into the RPF. Therefore, a

target RPF with fewer "on" points will appear brighter than one with many, assuming total energy is distributed approximately evenly between each "on" pixel in the RPF. As a result, a controller causes the intensity of the source to be modulated correspondingly to achieve a uniform overall brightness between frames, in accordance with the number of "on" points in each frame. Direct amplitude modulation of a laser is undesirable due to nonlinearity, and thus in an embodiment such amplitude modulation is replaced by pulse-width modulation within each 400 μ s pulse interval with a duty cycle proportional to the desired brightness to achieve the required average intensity.

10

Secondly, a design issue comes from the relationship between RPF size and illumination wavelength. This is overcome in one embodiment by a lens system corrected for chromatic aberration at the three wavelengths of the sources and in another by using Fresnel holography to build compensation for this effect directly into the holograms.

15

The results of the approach of the invention show in simulation a RPF exhibiting a noise energy of two orders of magnitude lower than direct binary search (DBS), with calculation times six orders of magnitude faster. Experimental results are in agreement with the theory, and show a previously undemonstrated level of contrast and accuracy for a holographically generated image even with a test device that is a very old design of ferroelectric SLM.

20

The invention has been described above in the context of binary operation and binary SLMs. However it will be understood that the algorithm itself is capable of extension to more than 2 phase levels.

25

An alternative to step 5 set out above is to use error diffusion. As known to those skilled in the art, Error Diffusion is a way of converting a continuous function to a

18

quantised function, whilst ensuring that the noise resulting from this operation is moved to an area of the replay field which does not impinge upon the desired image.

5 Although embodiments of the invention have been described, these are not limiting on the invention itself. This extends to the full scope of the appended claims.

CLAIMS

1. A method of displaying a holographically generated video image comprising plural video frames, the method comprising providing for each frame period a
5 respective sequential plurality of holograms and displaying the holograms of the plural video frames for viewing the replay field thereof, whereby the noise variance of each frame is perceived as attenuated by averaging across said plurality of holograms.
2. A method according to claim 1, wherein the providing step comprises
10 generating each hologram by implementing an algorithm having a single computationally intensive step.
3. A method according to claim 2, wherein the single step is a Fourier transform
15 step.
4. A method according to claim 3, wherein the algorithm is arranged, for each
said plurality of pixellated holograms, to:-
 - a) form first data having amplitude equal to the amplitude of the desired pixel;
 - b) inverse Fourier transform the first data to provide second data;
 - 20 c) shift the second data in the real direction in the complex plane sufficiently to form a third data set in which the phase of each data point is small;
 - d) form as a fourth data set the magnitude of the third data set; and
 - e) binarise the fourth data set to form a fifth data set for display as a said
25 hologram.
5. A method according to claim 4 wherein the step of binarisation comprises
thresholding about the median of the fourth data set whereby the fifth data set has dc
balance and low reconstruction error

6. A method according to claim 4 or 5, wherein the display device comprises a spatial light modulator having a pixellated phase mask imposing phase shifts of 0 and $\pi/2$, wherein the algorithm is arranged to generate a four-phase hologram, wherein each pixel has one of the values $[I, j, -I, -j]$
- 5
7. A method according to claim 6, wherein the pixel values of the phase mask are spatially random.
8. A method according to claim 7, wherein step b) comprises inverse Fourier
- 10 transforming and applying the phase mask values to the first data to provide the second data.
9. A method according to any preceding claim wherein the image is a 2 dimensional image.
- 15
10. A method according to claim 3 or any claim dependent upon claim 3, further comprising forming both the real and imaginary parts of the inverse Fourier transformed first data to form two second data sets, whereby two holograms are created per Fourier transform step.
- 20
11. Apparatus constructed and arranged to display a holographically generated video image having plural video frames, the apparatus having processing means arranged to provide for each frame period a respective sequential plurality of holograms and a display device arranged to receive the sequential plurality of
- 25 holograms of each frame and to display the holograms of the plural video frames of the video image for viewing the replay field thereof, whereby the noise variance of each frame is perceived as attenuated by averaging across said plurality of holograms.

12. Apparatus according to claim 11 wherein the processing means is arranged to generate each said hologram by implementing an algorithm having a single computationally intensive step.
- 5 13. Apparatus according to claim 12, wherein the single step is a Fourier transform step.
14. Apparatus according to claim 12, wherein the algorithm is arranged, for each said plurality of pixellated holograms, to:-
- 10 a) form first data having amplitude equal to the amplitude of the desired pixel;
b) inverse Fourier transform the first data to provide second data;
c) shift the second data in the real direction in the complex plane sufficiently to form a third data set in which the phase of each data point is small;
d) form as a fourth data set the magnitude of the third data set; and
- 15 e) binarise the fourth data set to form a fifth data set for display as a said hologram.
15. Apparatus according to claim 14, wherein the step of binarisation comprises thresholding about the median of the fourth data set whereby the fifth data set has dc
- 20 balance and low reconstruction error.
16. Apparatus according to claim 11,12 or 13, wherein the display device comprises a spatial light modulator having a pixellated phase mask imposing phase shifts of 0 and $\pi/2$, wherein the algorithm is arranged to generate a four-phase
- 25 hologram, wherein each pixel has one of the values $[1,j,-1,-j]$.
17. Apparatus according to claim 16, wherein the pixel values of the phase mask are spatially random.

18. Apparatus according to claim 17, wherein step b) comprises inverse Fourier transforming and applying the phase mask values to the first data to provide the second data.
- 5 19. Apparatus according to claim 14 or any claim dependent upon claim 14, further comprising forming both the real and imaginary parts of the inverse Fourier transformed first data to form two second data sets, whereby two holograms are created per Fourier transform step.
- 10 20. A method of generating pixellated holograms, the method comprising forming a first data set, the members of said first data set having respective amplitudes equal to the amplitudes of respective desired pixels;
performing an inverse Fourier transform on the first data set to provide second data set;
15 shifting the second data set in the real direction in the complex plane sufficiently to form a third data set in which the phase of each data point is small;
forming as a fourth data set the magnitude of the third data set; and
binarising the fourth data set to form a fifth data set for display as a said hologram:
20
21. A method according to claim 20 wherein the step of binarisation comprises thresholding about the median of the fourth data set whereby the fifth data set has dc balance and low reconstruction error.
- 25 22. A method according to claim 20 or 21, wherein the display device comprises a spatial light modulator having a pixellated phase mask imposing phase shifts of 0 and $\pi/2$, wherein the algorithm is arranged to generate a four-phase hologram, wherein each pixel has one of the values $[1, j, -1, -j]$.

23

23. A method according to claim 20, wherein the pixel values of the phase mask are spatially random.
24. A method according to claim 20 or 21, further comprising applying the phase mask values to the first data to provide the second data.
25. A method according to any of claims 20-24, wherein the image is a 2 dimensional image.
26. A method according to any of claims 20-25, further comprising forming both the real and imaginary parts of the inverse Fourier transformed first data to form two second data sets, whereby two holograms are created per Fourier transform step.

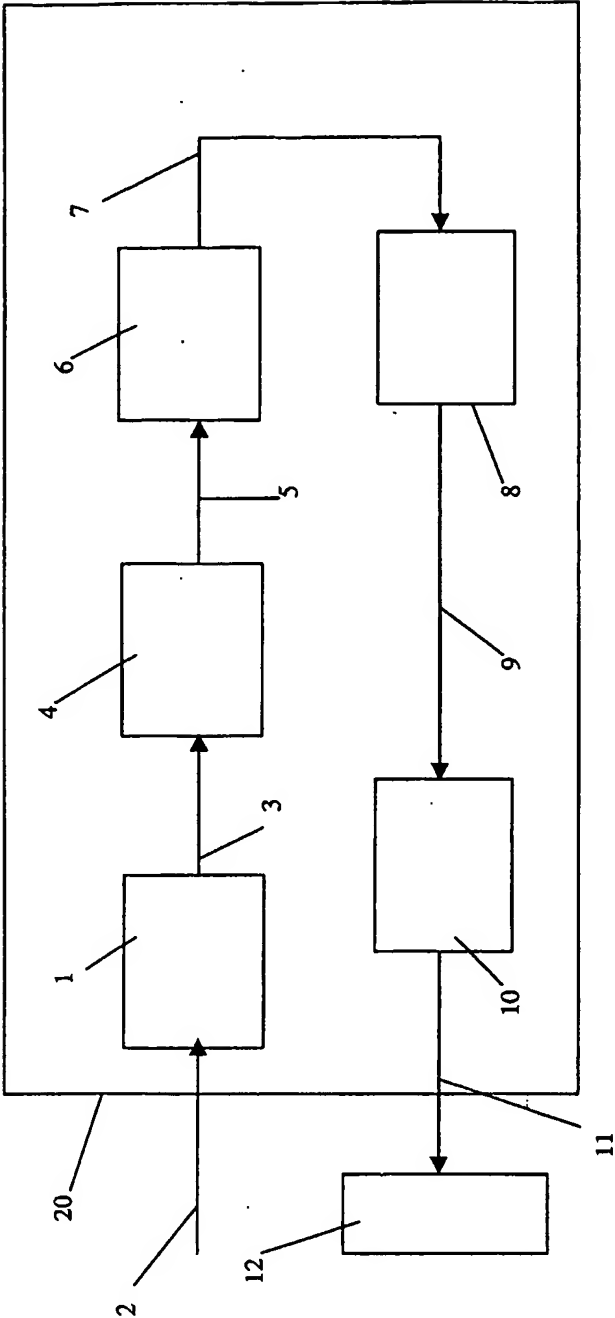


Figure 1

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Figure 2a



Figure 2b



Figure 2c



Figure 3a

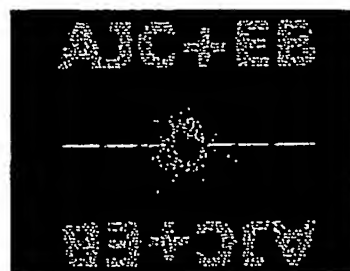


Figure 3b

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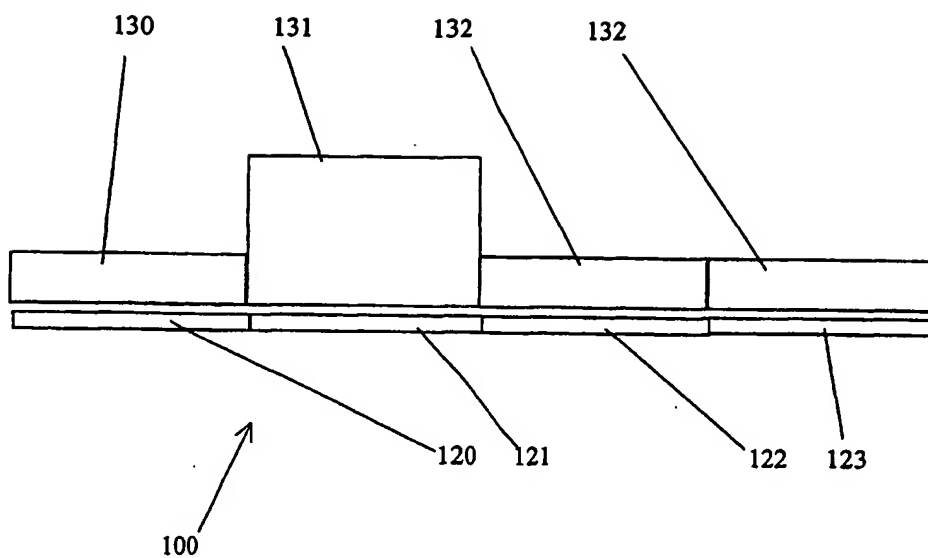


Figure 4

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